Midterm 1 October 12, 2016 Duration: 50 minutes

This test has 4 questions on 9 pages, each worth 10 points, for a total of 40 points.

- Read all the questions carefully before starting to work.
- Give complete arguments and explanations for all your calculations. Answers without justifications will not be marked, except question #3 where the answer alone is sufficient.
- Continue on the closest blank page if you run out of space.
- Attempt to answer all questions for partial credit.
- This is a closed-book examination. No aids of any kind are allowed, including: documents, cheat sheets, electronic devices of any kind (including calculators, phones, etc.)

First Name:	Last Name:
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Student-No: _

Section: _

Signature:

Question:	1	2	3	4	Total
Points:	10	10	10	10	40
Score:					

Student Conduct during Examinations 1. Each examination candidate must be prepared to produce, upon (ii) purposely exposing written papers to the view of other examination candidates or imaging devices; the request of the invigilator or examiner, his or her UBCcard for identification. (iii) purposely viewing the written papers of other examination candidates: Examination candidates are not permitted to ask questions of the examiners or invigilators, except in cases of supposed errors or am-(iv) using or having visible at the place of writing any books, pabiguities in examination questions, illegible or missing material, or pers or other memory aid devices other than those authorized the like. by the examiner(s); and, using or operating electronic devices including but not lim-3. No examination candidate shall be permitted to enter the examina-(v) ited to telephones, calculators, computers, or similar devices tion room after the expiration of one-half hour from the scheduled other than those authorized by the examiner(s)—(electronic devices other than those authorized by the examiner(s) must starting time, or to leave during the first half hour of the examination. Should the examination run forty-five (45) minutes or less, no examination candidate shall be permitted to enter the examination be completely powered down if present at the place of writroom once the examination has begun. ing). 4. Examination candidates must conduct themselves honestly and in 6. Examination candidates must not destroy or damage any examinaaccordance with established rules for a given examination, which will be articulated by the examiner or invigilator prior to the examiner α tion material, must hand in all examination papers, and must not take any examination material from the examination room without ination commencing. Should dishonest behaviour be observed by the examiner(s) or invigilator(s), pleas of accident or forgetfulness permission of the examiner or invigilator. shall not be received. Notwithstanding the above, for any mode of examination that does 7. not fall into the traditional, paper-based method, examination can-Examination candidates suspected of any of the following, or any didates shall adhere to any special rules for conduct as established other similar practices, may be immediately dismissed from the examination by the examiner/invigilator, and may be subject to and articulated by the examiner. disciplinary action: Examination candidates must follow any additional examination (i) speaking or communicating with other examination candirules or directions communicated by the examiner(s) or invigiladates, unless otherwise authorized; tor(s).

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2 marks 1. (a) Consider the three points A = (0, 1, 1), B = (2, 1, 0), C = (3, -1, 2). Find the cosine of the angle between the vectors \overrightarrow{AB} and \overrightarrow{AC} .

Answer:

2 marks

(b) Continuing from previous part, find a normal vector to the plane containing the points A, B and C.

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3 marks (c) Find the equation of the line (in symmetric form) which is at the intersection of the planes 3x - 4y + 2z = -7 and 3x - 2y + 4z = -5

Answer:

3 marks

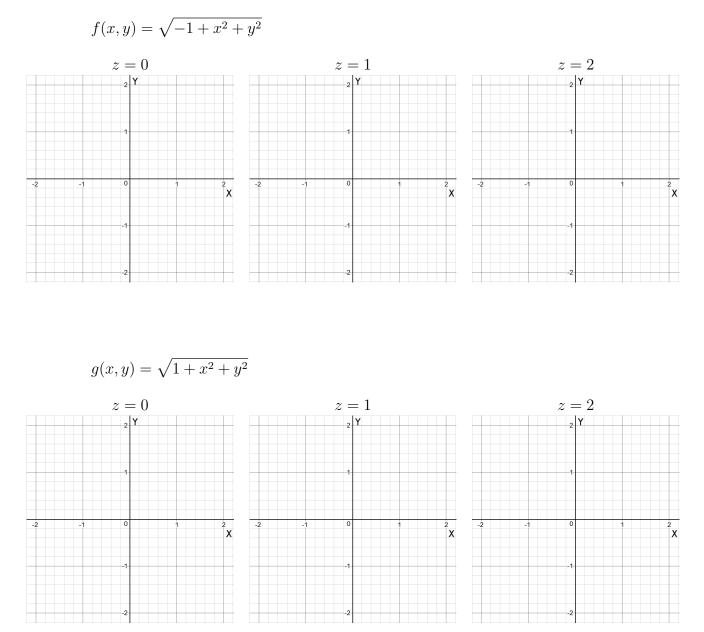
(d) Find the equations of all the planes that are at distance 1 unit from the plane x + y - z = 1.

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4 marks 2. (a) Let $f(x, y) = ye^{2x-y}$	$+4x\sin(y)+3x^2$. Compute t	the partial derivatives f_x and f_y .
	Answer:	

6 marks

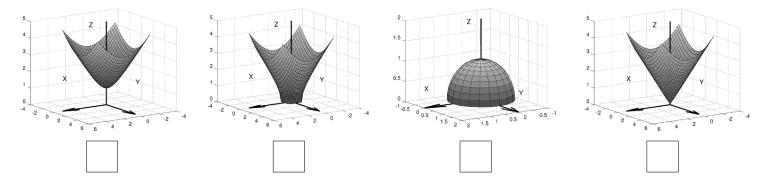
(b) Find all values of the constant c such that $g(t,x) = e^{-4t} \sin(cx)$ satisfies the heat equation $g_t = g_{xx}$.

8 marks 3. (a) On the axes provided, draw the level curves of z = f(x, y) at z = 0, 1 and 2 for the following functions. (Note: only those axes will be graded.)



2 marks

(b) Of the four graphs pictured below, identify which is a graph of f(x, y) and which is a graph of g(x, y) by writing f or g beneath the appropriate graph.



4. Suppose we are interested in $w(a, b, c) = \frac{c^2}{ac - b}$ near $(a_0, b_0, c_0) = (1, 3.9, 4)$.

4 marks

(a) Near (a_0, b_0, c_0) , the function w is most sensitive to changes in which variable? Briefly justify your answer.

Answer:

2 marks

(b) Construct the best linear approximation to w near (a_0, b_0, c_0) .

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2 marks (c)	Assuming that each comp	ponent could vary by up	to 0.1 away from (a_0, b_0, c_0) .	what

is the maximum value attained by the linear approximation in part (b)?

Answer:

2 marks

(d) Still assuming that each component is within 0.1 of (a_0, b_0, c_0) , how large can the actual value of w become? Briefly justify your answer.

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